

Name: ANSWER KEY

Score: _____

For $f(x) = x^5 + x^4 - 6x^3 - 14x^2 - 11x - 3$

1 change of sign

$f(-x) = -x^5 + x^4 + 6x^3 - 14x^2 + 11x - 3$

4 changes of sign

- a. (6) use Descartes' rule of signs to determine the possible numbers of positive, negative, and non-real complex roots;

| | | | |
|-----|---|---|---|
| Deg | 5 | 5 | 5 |
| Pos | 1 | 1 | 1 |
| Neg | 4 | 2 | 0 |
| Cx | 0 | 2 | 4 |

- b. (4) find the best upper bound and best lower bound for the real roots.

| | | | | | | | |
|----|---|----|----|-----|-----|-----|--------------------------------------|
| | 1 | 1 | -6 | -14 | -11 | -3 | |
| 3 | 1 | 4 | 6 | 4 | 1 | 0 | $\therefore 3$ is upper bound & root |
| -3 | 1 | -2 | 0 | -14 | 31 | -96 | $\therefore -3$ is lower bound. |